

Important Discrete Random Variables

Name	Description	Assumptions	Distribution	Mean	Variance
Binomial	The number of successes in n Bernoulli trial.	<ol style="list-style-type: none"> Each trial is either a success or a failure. The probability of a success p is constant for each trial. All n trials are independent. 	$P(X = k) = \binom{n}{k} p^k q^{n-k}$ $k = 0, 1, 2, \dots, n$ $q = 1 - p$	np	npq
Poisson	The number of times an event occurs in a given unit of time or space. It can be used to approximate a Binomial when n is large and $\lambda = np$ is small.	<ol style="list-style-type: none"> The average rate of occurrences ($\lambda > 0$) is known. Events occur independently. 	$P(X = k) = \frac{e^{-\lambda} \lambda^k}{k!}$ $k = 0, 1, 2, \dots$	λ	λ
Geometric	The number of failures prior to the first success in a sequence of Bernoulli trials.	<ol style="list-style-type: none"> Each trial is either a success or a failure. The probability of a success p is constant for each trial. All trials are independent. The sequence of trials ends after the first success. 	$P(X = k) = pq^k$ $k = 0, 1, 2, \dots$ $q = 1 - p$	$\frac{q}{p}$	$\frac{q}{p^2}$
Negative Binomial	The number of failures prior to the r th success in a sequence of Bernoulli trials.	<ol style="list-style-type: none"> Each trial is either a success or a failure. The probability of a success p is constant for each trial. All trials are independent. The sequence of trials ends after the rth success. 	$P(X = k) = \binom{k+r-1}{k} p^r q^k$ $k = 0, 1, 2, \dots$ $q = 1 - p$	$\frac{rq}{p}$	$\frac{rq}{p^2}$
Hypergeometric	The number of successes in a sample of size n .	Sampling is done without replacement from a finite set of size N containing M successes and $N - M$ failures. We let $p = M/N$ and $q = 1 - p$.	$P(X = k) = \frac{\binom{M}{k} \binom{N-M}{n-k}}{\binom{N}{n}}$ $\max(0, n + M - N) \leq k$ $k \leq \min(n, M)$	np	$npq \left(\frac{N-n}{N-1} \right)$